



Province of the
EASTERN CAPE
EDUCATION

**NATIONAL
SENIOR CERTIFICATE**

GRADE 11

MATHEMATICS – THIRD PAPER

MEMORANDUM

NOVEMBER 2009

MARKS: 100

TIME: 2 hours

This memorandum consists of 8 pages.

QUESTION 1				
1.1	1.1.1	<p>P(that no jobs will be lost)</p> $= 1 - (0,5 + 0,2 + 0,05)$ $= 0,25$ <p>OR by using a Venn diagram</p>	(2)	<p>✓ Formula</p> <p>✓ answer</p>
	1.1.2	<p>Job losses in production and management sections are mutually inclusive because $P(P \text{ and } M) \neq 0$</p>	(2)	<p>✓ mutually inclusive</p> <p>✓ $P(P \text{ and } M) \neq 0$</p>
1.2	1.2.1	$a = 5 \quad b = 10 \quad c = 120 \quad d = 55 \quad e = 50 \quad f = 110$	(3)	<p>✓✓✓ answers (1 mark per two values)</p>
	1.2.2	<p>$P(\text{worthy of Permanent}) \times P(\text{production line A})$</p> $= \frac{110}{120} \times \frac{65}{120} = 0,4965 \dots$ <p>$P(\text{worthy of Permanent appointment and production line A})$</p> $= \frac{60}{120} = 0,5$ <p>NO. It is independent because the answers above are very close.</p>	(4)	<p>✓ answer</p> <p>✓ answer</p> <p>✓ NO/independent</p> <p>✓ reason</p>
			[11]	

QUESTION 2			
2.1	<pre> graph LR Meals --> B Meals --> H Meals --> P B --> BT[T] B --> BF[F] H --> HT[T] H --> HF[F] P --> PT[T] P --> PF[F] BT --> BTC[C] BT --> BTS[S] BF --> BFC[C] BF --> BFS[S] HT --> HTC[C] HT --> HTS[S] HF --> HFC[C] HF --> HFS[S] PT --> PTC[C] PT --> PTS[S] PF --> PFC[C] PF --> PFS[S] </pre>	(6)	✓ branch BTC and BTS ✓ branch BFC and BFS ✓ branch HTC and HTS ✓ branch HFC and HFS ✓ branch PTC and PTS ✓ branch PFC and PFS
2.2	There are $3 \times 2 \times 2 = 12$ different combinations.	(1)	✓ answer = 12
2.3	$P(\text{B and F}) = \frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$ OR $P(\text{B and F}) = \frac{2}{12} = \frac{1}{6}$	(2)	✓ rule ✓ answer
		[9]	

QUESTION 3			
3.1	<p>A Venn diagram with three overlapping circles labeled SK, FR, and ST, all contained within a universal set S. The regions are labeled with their respective counts: SK only is $19 - x$, FR only is $17 - x$, and ST only is 8. The intersection of SK and FR is x, SK and ST is 14, FR and ST is 11, and the intersection of all three is 7.</p>	(8)	<ul style="list-style-type: none"> ✓ for 7 ✓ for 12 ✓ for 14 ✓ for 11 ✓ for x ✓ for $19 - x$ ✓ for $17 - x$ ✓ for 8
3.2	Workers who did not take any of the three mentioned type of leave = $(80 - 68) = 12$.	(1)	✓ answer
3.3	Workers who took sick leave and family responsibility leave but not study leave are equal to x . $\therefore 19 - x + 17 - x + 14 + 7 + 11 + 8 + x = 68$ $76 - x = 68$ $x = 8$	(3)	<ul style="list-style-type: none"> ✓ equation ✓ simplification ✓ answer
			[12]

QUESTION 4				
4.1	4.1.1	There were $100\,000 - 20\,000 = 80\,000$ new jobs created between January and March.	(1)	✓ answer
	4.1.2	No. Fewer jobs were created each month from February to June. The number of new jobs being created is actually decreasing. OR Yes. 100 000 new jobs were created from January to June.	(3)	✓ No ✓ ✓ explanation
4.2	4.2.1	In 2011 the price of bread will be $(R8,00 + R1,50) = R9,50$. Also accept $(R8,00 + 23\% \times R8,00) = R9,85$	(1)	✓ answer
	4.2.2	The scale on the y-axis does not start at zero, as well as the interval used on the y-axis. The effect is that the bread price is rising more steeply than is the case.	(2)	✓ does not start at 0 ✓ conclusion
4.3	4.3.1	30	(1)	
	4.3.2	Skewed to the right.	(1)	
	4.3.3	Numbers above and below are equal.	(1)	
	4.3.4	75%	(1)	
	4.3.5	The grade 12 class: inter-quartile range is smaller for the grade 12 class.	(2)	
			[13]	

QUESTION 5			
5.1		Total number of workers who prefer to do a management course = $\frac{12}{60} \times 2\,000 = 400$ workers	(2) ✓ calculation ✓ Answer
5.2		No. Sample is too small (3% only). Sample should be at least 10% of the total number of workers.	(3) ✓ No ✓✓ Explanation
			[5]
* FOR QUESTIONS 6 TO 8 FOLLOW THE CANDIDATE'S REASONING *			
QUESTION 6			
6.1		PQRS is similar to ABCD – sides are proportional	(2) ✓ statement ✓ reason
6.2	6.2.1	$\frac{AB}{PB} = \frac{AC}{QC}$ $QC = \frac{6 \times 2}{8} = \frac{12}{8} = \frac{3}{2} \text{ mm}$	(4) ✓✓ ratios ✓ substitution ✓ answer
	6.2.2	$\frac{BC}{PQ} = \frac{AB}{AP}$ $BC = \frac{8 \times 7,5}{6} = 10 \text{ mm}$	(4) ✓✓ ratios ✓ substitution ✓ answer
	6.2.3	$AB^2 = 8^2 = 64$; $AC^2 = 6^2 = 36$; $BC^2 = 10^2 = 100$ $\therefore \triangle ABC$ is a right-angled triangle (satisfies Theorem of Pythagoras)	(3) ✓ side lengths ✓ Pythagoras ✓ conclusion
			[13]

QUESTION 7			
7.1	7.1.1	<p>In $\triangle ABP$ and $\triangle CBA$ \hat{B} is common $\hat{A}PB = \hat{C}AB = 90^\circ$ (given) $\hat{P}AB = \hat{C}CB$ (third angle)</p> <p>$\therefore \triangle ABP \text{ /// } \triangle CBA$ ($\angle\angle\angle$)</p>	<p>✓ statement ✓ statement</p> <p>✓ reason or third angle</p>
			(3)
	7.1.2	$\frac{AB}{CB} = \frac{AP}{CA}$ <p>$\therefore AB \times CA = AP \times CB$</p>	<p>✓✓ one per ratio</p> <p>✓ cross multiplication</p>
			(3)
7.2	7.2.1	$\frac{b+6}{c} = \frac{4\sqrt{5}}{6\sqrt{5}} \left(= \frac{2}{3} \right)$ $2c = 3b + 18$ $c = \frac{3b+18}{2}$	<p>✓✓ ratios</p> <p>✓ cross multiplication</p> <p>✓ answer</p>
			(4)
	7.2.2	$\frac{b}{6} = \frac{4\sqrt{5}}{6\sqrt{5}} \left(= \frac{2}{3} \right)$ $3b = 12$ $b = 4 \text{ cm}$	<p>✓ ratio</p> <p>✓ cross multiplication</p> <p>✓ answer</p>
			(3)
	7.2.3	$c = \frac{3(4) + 18}{2} = 15 \text{ cm}$	<p>✓ answer</p>
			(1)
	7.2.4	<p>$\triangle PUT \text{ /// } \triangle RVT$ $\hat{P} = \hat{R}$ ($PQ = QR$) $\hat{P}UT = \hat{R}VT$ (both = 90°)</p> <p>$\therefore \frac{VR}{PU} = \frac{TR}{PT}$</p> $VR = \frac{4 \times 6\sqrt{5}}{4\sqrt{5}}$ $VR = 6 \text{ cm}$	<p>✓ $\triangle PUT \text{ /// } \triangle RVT$ ✓ reasons</p> <p>✓ ratios =</p> <p>✓ substitution</p> <p>✓ answer</p>
			(5)
			[19]

QUESTION 8				
8.1	8.1.1	Parallel to	(1)	✓ answer
	8.1.2	Similar/equiangular	(1)	✓ answer
8.2	8.2.1	$\frac{AP}{AB} = \frac{1}{2} \quad ; \quad \frac{AT}{AS} = \frac{1}{2} \quad ; \quad \frac{PT}{BS} = \frac{1}{2}$ $\therefore \triangle APT \sim \triangle ABS \text{ [sides in proportion]}$	(4)	✓ ratio ✓ ratio ✓ ratio ✓ reason
	8.2.2	$\hat{A}TP = \hat{A}SB \text{ [triangles similar]}$ $\therefore PT \parallel BS \text{ [corresponding angles equal]}$ <p>OR may use the Midpoint Theorem</p>	(2)	✓ statement ✓ reason
	8.2.3	$\frac{CS}{CT} = \frac{CR}{CQ} \text{ [SR \parallel TQ]}$ $= \frac{1}{3}$	(3)	✓ statement/ ratios ✓ reason ✓ answer
	8.2.4	$\triangle CSR \sim \triangle CTQ \text{ [equiangular]}$ $\frac{SR}{TQ} = \frac{CR}{CQ} = \frac{1}{3}$	(3)	✓ similar triangles ✓ ratios ✓ answer
	8.2.5	$\frac{\text{Area of } \triangle CSR}{\text{Area of } \triangle CQT}$ $= \frac{\frac{1}{2} \times SR \times CS}{\frac{1}{2} \times TQ \times CT}$ $= \frac{SR}{TQ} \times \frac{CS}{CT}$ $= \frac{1}{3} \times \frac{1}{3}$ $= \frac{1}{9}$	(4)	✓ area top ✓ area bottom ✓ simplification ✓ substitution
			[18]	
			TOTAL:	100